

- I. For a binomial distribution where “p” (probability of success in any one trial) is not known, it may be estimated by a sampling distribution of \bar{p} using:
 - (1) standard normal distribution if σ is known
 - (2) t-distribution if σ is not known (not covered)
- II. The “margin of error” is $E = |\bar{p} - p|$; *i.e.*, how far “ \bar{p} ” is from the true (population) value for “p”
- III. The “confidence interval” for \bar{p} in a sampling distribution is given by: $\bar{p} - E < p < \bar{p} + E$, where the confidence level is expressed by a percent, $P(\bar{p} - E < p < \bar{p} + E) = c\%$...

IV. Using the standard normal distribution:

if $P(-z_c < z < z_c) \approx c\%$, then...

“E” can be determined as follows,

solve $z_c = (p + E - \mu_{\bar{p}}) \div \sigma_{\bar{p}}$


multiply by “ $\sigma_{\bar{p}}$ ”, to obtain

$$z_c \times \sigma_{\bar{p}} = p + E - \mu_{\bar{p}}$$

then use $\sigma_{\bar{p}} = \sigma \div \sqrt{n}$ & $\mu_{\bar{p}} = p$

to get $z_c \times \sigma \div \sqrt{n} = p + E - p$

$$z_c \times \sigma \div \sqrt{n} = E$$

 p.388

“ z_c ” is the “critical value”

and $\sigma = \sqrt{p(1-p)}$

V. The confidence interval/level & margin of error model is statistically valid provided:

(1) the binomial distribution is normally distributed

OR

(2) $n > 5 \div \bar{p}$ and $n > 5 \div (1 - \bar{p})$

VI. Examples (pp.395-398): #8,10a,**14ab**,22

HW: pp.395-398 / #1,3,7,9a,13ab,15,19

Read pp.401-412 (section 7.4)

I. Comparing two population means μ_1 & μ_2 , or two binomial percentages p_1 & p_2 , can be done provided that the:

(1) original/raw data are normally distributed;

OR

(2) original/raw data distribution is not highly skewed, and that the sampling distributions both have sample sizes no less than 30.

II. Difference of Population Means (pp.403-405):

$E = \text{critical value} \times \text{standard deviation}$

$$\sigma = \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} \quad (\text{provided on tests}) \quad \begin{array}{l} \text{use } s_1 \text{ \& } s_2 \\ \text{if } \sigma_1 \text{ \& } \sigma_2 \\ \text{unknown} \end{array}$$

Confidence interval:

$$(\bar{x}_1 - \bar{x}_2) - E < \mu_1 - \mu_2 < (\bar{x}_1 - \bar{x}_2) + E$$

III. Difference of Binomial Percentages (p.409):

$E = \text{critical value} \times \text{standard deviation}$

$$\bar{\sigma} = \sqrt{\frac{\bar{p}_1(1-\bar{p}_1)}{n_1} + \frac{\bar{p}_2(1-\bar{p}_2)}{n_2}} \quad (\text{provided on tests})$$

Confidence interval:

$$(\bar{p}_1 - \bar{p}_2) - E < p_1 - p_2 < (\bar{p}_1 - \bar{p}_2) + E$$

VI. Examples (pp.412-421): #**4,6,10,16b,28c**

HW: pp.412-420 / #1,5,7,11,15,21,28a

Read pp.438-449 (section 8.1)